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Abstract : This thesis is mainly concerned with the applications of the group: theoretical methods to boundary value problems. The general concept of Lie group is printed in Chapter 1. In Chapter 2 we demonstrate the applications of the group theoretical methods to the following boundary value problem $n(n+1)f''(z) - j(z)[j''(z)]r^{-n} = 0$, (1) under the boundary conditions $j(0) = j(\infty) = 0$, $j'(0) = 1$. (2) We shall call equation (1) the Generalized Blasius equation (GB equation) which describes the boundary layer of a non-Newtonian fluid near a semi infinite flat plate, where n is a given constant. In this chapter we obtain for any n (included the value $n = 1$ investigated before in [6]) the following results (i) The symmetry groups of (1), (ii) The invariant solutions of (1), (iii) New solutions from known solution for (1), (iv) Reduce the order of (1) to a first order ordinary differential equation, (v) Transform the GB boundary value problem to an initial value problem. In Chapter 3 we develop a simple technique in attempting to give an approximate analytical solution for the GB boundary value problem. The proposed solution for the value of $0 < n < 2$ (the practical values of n) gives results better than the results obtained using Pohlhausens integral method [1] and very good agreement with the results of exact numerical treatment obtained by Acrivos [1]. In Chapter 4 we use the invariant solutions to obtain a solution for the linear heat conduction equation under the third type of boundary conditions. In practice this problem is known as Stokes first problem with slip velocity at boundary

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